

## Low-Energy Electron Diffractometry from the Cleavage Face (001) of Magnesium Oxide

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With a triple-axis low-energy electron diffractometer, the intensity curves of the specular reflexion 00 from the cleaved face (001) of a MgO crystal were measured against the glancing angle, for the electrons in the energy range from 180 eV to 500 eV and for three crystal azimuths in a range near [010]. By the use of diagrams drawn on the basis of the Ewald construction to indicate the surface wave resonance conditions for various reciprocal rods, a number of fine structures as well as gross features of the intensity curves were interpreted fairly well in terms of the resonance effect.

### 1. Introduction

The intensity curve of low-energy electron diffraction (LEED), obtained either by the variable-energy method or the constant-energy method, shows in most cases complicated features which require theoretical calculations of high approximation to interpret the details. Recent theoretical calculations, for instance those by Jepsen, Marcus & Jona (1972) and Pendry (1971*a,b*), succeeded fairly well in reproducing some examples of the intensity curves experimentally obtained. However, these calculations are not always suitable to give a ready physical understanding about the origin of individual anomalies in an intensity curve.

As a rule, an intensity curve of LEED, *e.g.* that obtained by the constant-energy method, changes sensitively with the variation of the electron energy and/or the crystal azimuth, and also extra peaks sometimes appear at off-Bragg positions. As pointed out in a previous paper (Miyake & Hayakawa, 1970), some of the anomalous behaviour in the LEED intensity curves can be ascribed to the 'resonance effect' [or Kikuchi-Nakagawa effect (Kikuchi & Nakagawa, 1933)]. This effect is a diffraction phenomenon in LEED which takes place when a Bragg reflexion (a surface wave) is excited in a direction parallel or nearly parallel to the crystal surface (McRae, 1966; McRae & Caldwell, 1967), and is essentially the same effect as Kikuchi & Nakagawa's anomaly known in HEED (Miyake & Hayakawa, 1970). As this effect may take place frequently in LEED, it is expected that the intensity curve in LEED may be affected by the resonance effect, not only partly but also with respect to the overall feature.

The present paper is concerned with the intensity measurement of the 00 reflexion from the cleavage surface (001) of the MgO crystal using the constant-energy method for various energies of the electrons, and the details of the intensity curves obtained were investigated with special reference to the resonance effect.

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### 2. Instrumental

In order to investigate the resonance effect in LEED, and also for more general purposes in LEED studies, a low-energy electron diffractometer with three rotating axes, as shown schematically in Fig. 1, was constructed. The radius of the fluorescent screen, made of surface-conductive glass, was 100 mm, the spacing between  $G_1$  and  $G_2$  was about 5 mm, and the receiving aperture of the Faraday cage was 4 mm  $\varnothing$ .‡

‡ This apparatus can also be used for the electron diffraction experiments in the medium energy range of 1–5 keV (MEED).

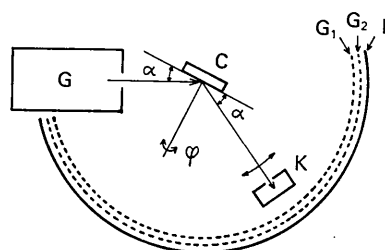


Fig. 1. Schematic diagram of a low-energy electron diffractometer. *G*, low-energy electron gun; *C*, crystal specimen; *K*, Faraday cage;  $G_1$ ,  $G_2$ , cylindrical metal mesh electrodes; *F*, cylindrical fluorescent screen.  $\alpha$ , glancing angle;  $\varphi$ , azimuthal angle.

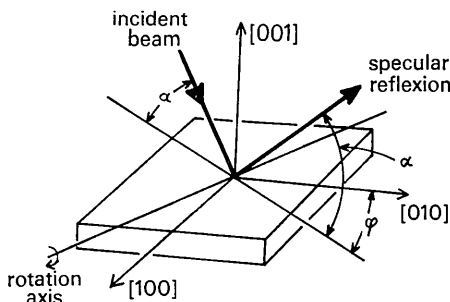


Fig. 2. Definition of the glancing angle  $\alpha$  and the azimuthal angle  $\varphi$ .

The specimen crystal *C* and the Faraday cage *K* can be rotated either independently or in the  $\alpha-2\alpha$  relation around an axis perpendicular to the figure plane, where  $\alpha$  is the glancing angle of the incident beam to the crystal surface. Rotation of these parts was operated from the outside of the vacuum. The smallest angular step of  $\alpha$  was  $0.05^\circ$ . The azimuthal angle  $\varphi$  of the crystal was changed by rotating the specimen holder around an axis perpendicular to the crystal surface, and this angle was fixed as desired before each intensity measurement.

The diffractometer unit composed of these parts was enclosed in a vacuum chamber consisting of a glass bell-jar, which was connected to an ion sputtering pump. The operating pressure was in the range of  $10^{-8}$  torr. This vacuum condition was enough to maintain the surface of MgO crystal free from contamination due to the electron irradiation.

### 3. Intensity measurement

The MgO specimen was prepared by cleaving a MgO single crystal in air. The area of the cleaved surface, about  $10 \times 20$  mm, was sufficient to receive the whole

beam even at the smallest range of the glancing angle. The intensity curve of the specular reflexion 00 was obtained as a function of the glancing angle  $\alpha$  for various values of the electron energy  $E_p$  and the azimuthal angle  $\varphi$ . The glancing angle  $\alpha$  and the azimuthal angle  $\varphi$  were defined as shown in Fig. 2. Each intensity measurement was performed by first setting the Faraday cage at the correct position to receive the specular reflexion, and then rotating the specimen and the Faraday cage together in the  $\alpha-2\alpha$  relation, over an angular range of  $\alpha$  from 0 to  $75^\circ$ . The electron energy was changed every 40 eV step in the range from 180 to 500 eV. The crystal azimuths studied were:

$$\begin{aligned} A \text{ ([010]-azimuth): } & \varphi = 0^\circ, \\ B: & \varphi = 5^\circ, \\ C: & \varphi = 10^\circ. \end{aligned}$$

Fig. 3(a)–(c) shows the intensity curves thus obtained. The abscissa in each Figure is the glancing angle  $\alpha$  and the ordinate is the reflected intensity normalized by the primary beam current which was of the order of  $0.5 \mu\text{A}$ . The maximum current of the re-

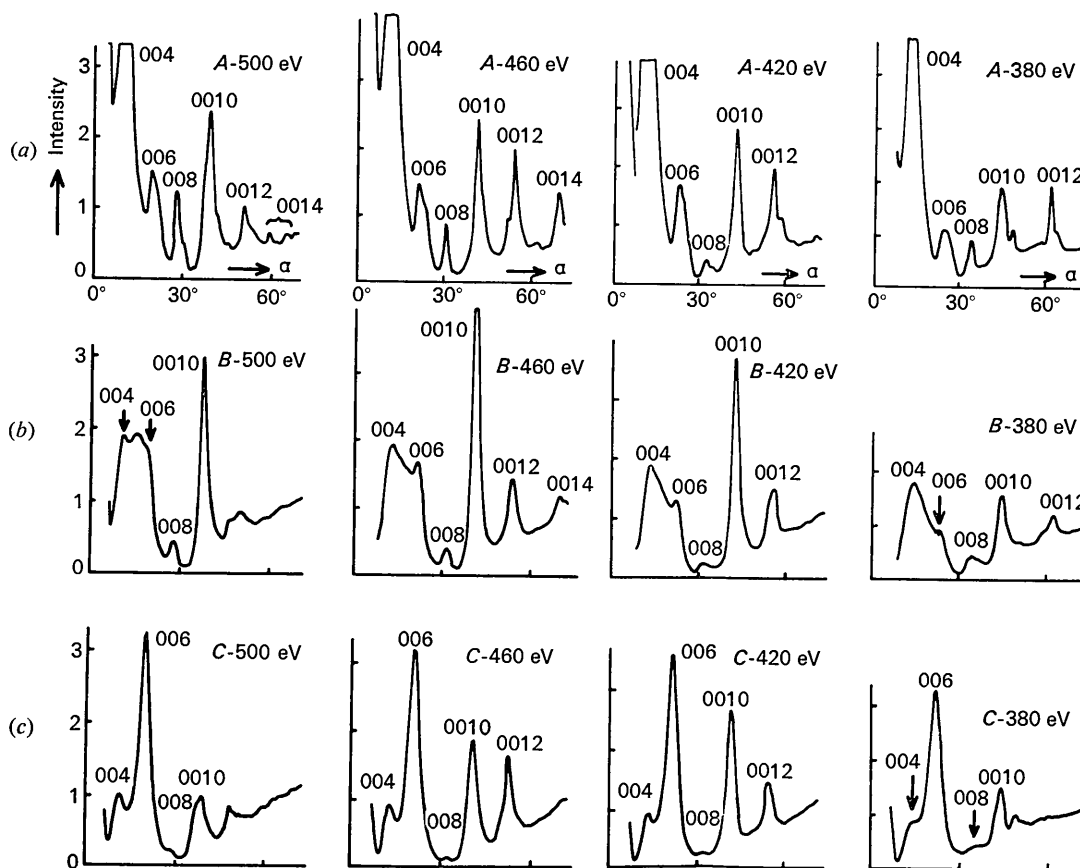


Fig. 3. Intensity curves of the specular reflexion for various electron energies  $E_p$  obtained from a MgO single-crystal cleavage surface. Abscissa: the glancing angle  $\alpha$ , ordinate the reflexion intensity. Each interval between horizontal bars on the ordinates corresponds to the normalized intensity  $2.5 \times 10^{-3}$ .

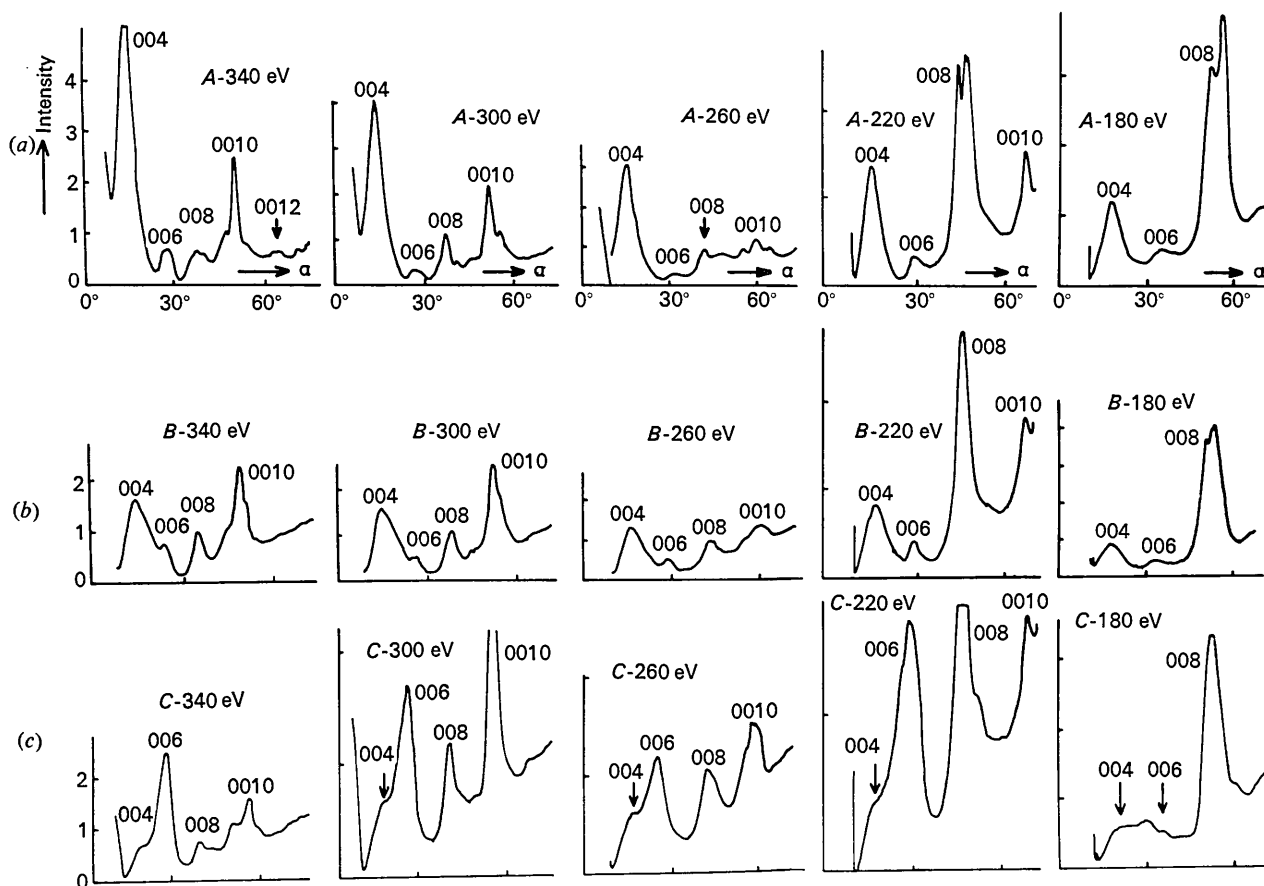


Fig. 3 (cont.)

flexion spot was of the order of  $10^{-2}$  times the primary current. Hereafter, each curve in Fig. 3, e.g. that for the *A*-azimuth and 500 eV electrons, is designated as *A*-500 eV.

In addition to the intensity measurement described above, visual and photographic pattern observations were performed. The pattern observation was useful in giving the relation between the intensity behaviour of the 00 spot and the overall feature of the diffraction pattern. Figs. 4–8 are examples of the photographic patterns, which were obtained at the glancing angles indicated in each of the accompanying intensity curves.

#### 4. Resonance condition

##### (a) Ewald construction

The resonance effect takes place when a diffracted beam is excited in a direction parallel or nearly parallel to the crystal surface. This condition can be obtained by the Ewald construction, as follows.

When, for instance, the specular reflexion 00 satisfies the Bragg condition 004 for a given incident beam in the [010] azimuth (*A*-azimuth), the surface waves  $20\bar{2}$  and  $\bar{2}02$  are additionally excited since the reciprocal-

lattice points  $20\bar{2}$  and  $\bar{2}02$  come to lie on the horizontal great circle of the Ewald sphere. In this case, the reciprocal rods  $20$  and  $\bar{2}0$  are tangential to the Ewald sphere at the points  $20\bar{2}$  and  $\bar{2}02$ . In other words, these vertical rods intersect perpendicularly the horizontal great circle which is in the plane parallel to the crystal surface (001) and passing through the centre of the sphere *A*, as shown in Fig. 9. We may say that, under the assumed condition both the  $20$ -rod resonance and the  $\bar{2}0$ -rod resonance take place simultaneously with the 004 Bragg reflexion.

As illustrated by the above example, the resonance condition, or the condition for each rod resonance, can generally be obtained by finding out the condition that a vertical reciprocal-lattice rod intersects the horizontal great circle of the Ewald sphere. Fig. 10 shows this circle and the intersecting points with the figure plane of the vertical rod array for the MgO crystal with the cleavage surface (001). The radius of the Ewald sphere and, accordingly that of the horizontal great circle, is assumed to be  $\kappa_0 = n_0 K$ , where  $K = 1/\lambda$ ,  $\lambda$  is the electron wavelength in free space,  $n_0$  is the mean refractive index of the crystal for the electrons and is equal to  $(1 + eV_0/E_p)^{1/2}$ , where  $E_p$  is the electron energy,  $V_0$  is the

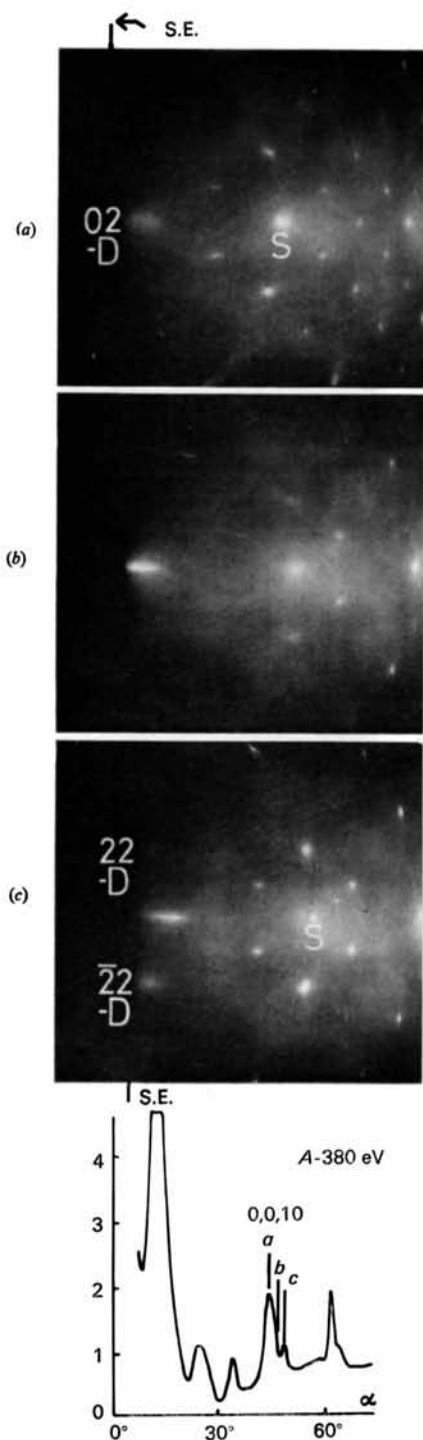


Fig. 4. Diffraction patterns in which the specular reflexion  $S$  is nearly at the condition of  $0,0,10$  peak in  $A-380$  eV. S.E.; the shadow edge. The  $02$ -rod resonance takes place in the vicinity of (a), in which the  $02$  diffuse spot ( $02-D$ ) begins to appear above the shadow edge. The  $22$ -rod resonance takes place at (c), in which the  $22$ -diffuse spot ( $22-D$ ) is observed.

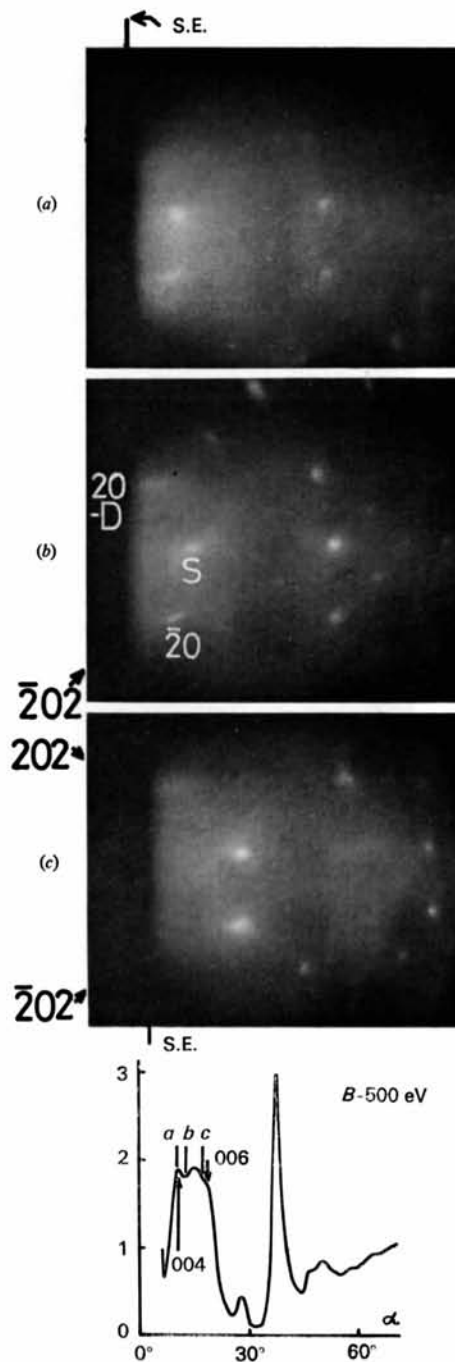


Fig. 5. Diffraction patterns in the range of the lowest order peak in  $B-500$  eV. The  $20$ -rod resonance condition is satisfied in the vicinity of (b), in which the specular reflexion  $S$  lies on the Kikuchi line  $\bar{2}02$  and also a diffuse spot ( $20-D$ ) belonging to the  $20$  rod begins to appear.

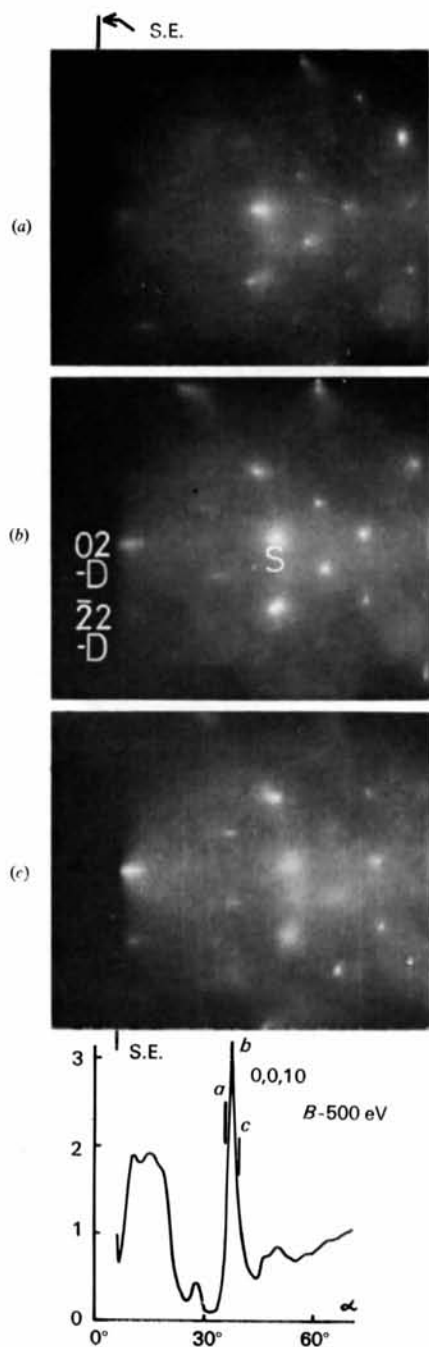


Fig. 6. Diffraction patterns in  $B-500 \text{ eV}$ . S.E.; the shadow edge. The specular reflexion  $S$  in the range of the Bragg condition  $0,0,10$  is enhanced by the  $02$ -rod resonance. The  $02$ -rod diffuse spot ( $02-D$ ) is observed at the shadow edge in (b). Successive occurrence of the  $02$ - and  $22$ -rod resonances can be known from the appearance of the corresponding diffuse spots by a slight change of the glancing angle.

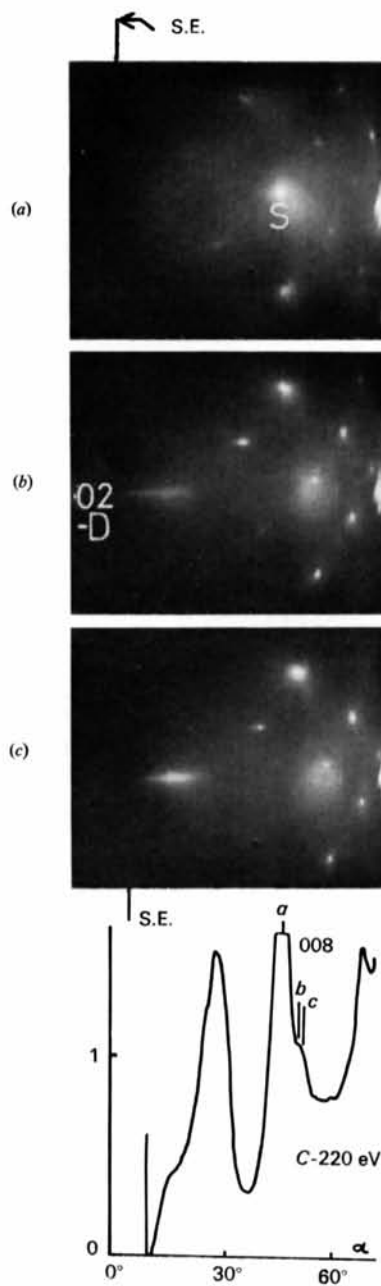


Fig. 7. Diffraction patterns in  $C-220 \text{ eV}$ . The specular reflexion  $S$  satisfying the Bragg condition  $008$  is remarkably enhanced in (a) and, correspondingly, the appearance of the  $02$ -rod diffuse spot ( $02-D$ ) is observed in (b), showing that the intensity enhancement of  $S$  is due to the  $02$ -rod resonance.

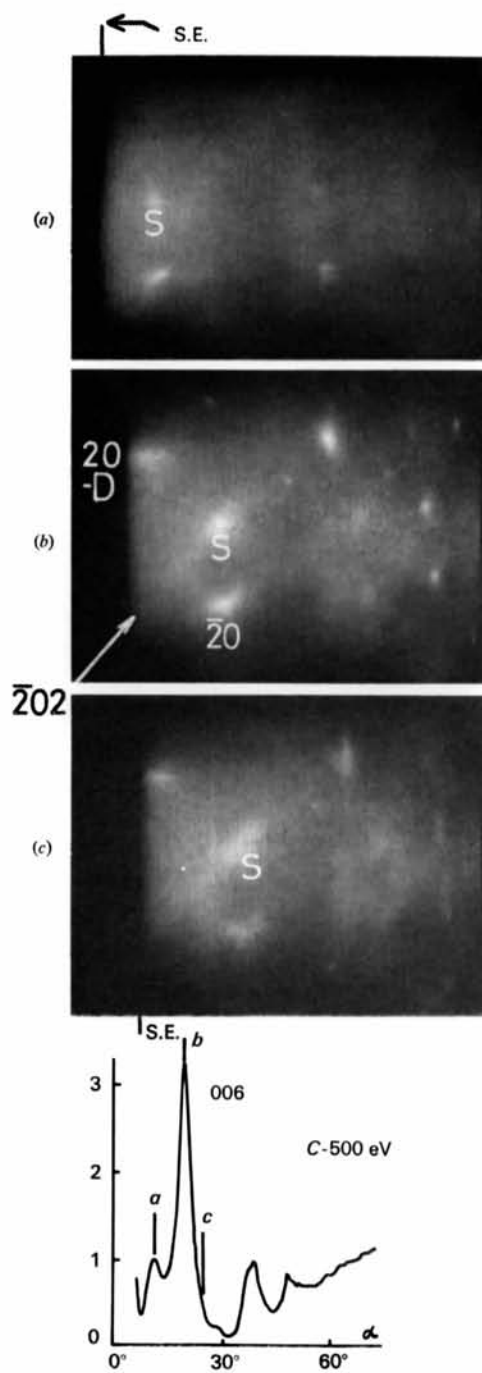


Fig. 8. Diffraction patterns in C-500 eV. In (b) the Kikuchi line  $\bar{2}02$  passes through the spot S and the 20-rod diffuse spot is simultaneously observed, indicating that the intensity of the specular reflexion satisfying the Bragg condition 006 is enhanced by the 20-rod resonance. It should also be noticed that the intensity of each diffraction spot is abruptly weakened in the photograph (c).



### 5. Interpretation of the intensity curves

In the present section it is shown by some typical examples that important features of the intensity curves in Fig. 3 may be understood in terms of the resonance curves in Fig. 11.

#### (a) Fine structures

Fig. 12 illustrates an example in which a fairly complicated fine structure of an intensity curve can be interpreted as a group of intensity peaks corresponding to a number of rod resonances. Fig. 12(a) is a part of the intensity curve *A*-260 eV in Fig. 3, and (b) corresponds to the relevant part of Fig. 11(a), drawn as a function of  $\alpha$  assuming the mean inner potential to be  $V_0 = 14$  V. By comparison of the two Figures, it is evident that the peak *a* is the 008 Bragg reflexion affected by the simultaneous resonances for the 40 and  $\bar{4}0$  rods, the peak *d* is the 0,0,10 Bragg reflexion, and the peaks *b*, *c* and *e* are no doubt the extra intensity maxima corresponding to the 02-rod, 22-rod +  $\bar{2}2$ -rod, and 42-rod +  $\bar{4}2$ -rod resonances, respectively. Although there are some discrepancies between the peak positions and the resonance conditions given by the resonance curves, the correspondence between them can be confirmed by inspecting the systematic change of the intensity curve with the electron energy. Most fine structures found in the intensity curves for the *A* azimuth can be explained in the similar way. Fig. 13 is another example, where (a) is a part of *A*-380 eV in Fig. 3 and (b) corresponds to the relevant part of Fig. 11(a). It is noted that there is a close coupling between the Bragg reflexion 0,0,10 and the 02-,  $\bar{2}2$ - and 22-rod resonances (cf. Fig. 4).

A similar analysis is also applicable to the intensity curves for the *B* and *C* azimuths. Fig. 14 is concerned with the fine structure of the lowest order peak in the intensity curve *B*-500 eV in Fig. 3. This peak is found to be a combination of the 004 and 006 Bragg reflexions and the peak due to the 20-rod resonance (cf. Fig. 5). In this connexion, it is interesting to note that the peak profile in this case is quite similar to that of the lowest-order peak in the intensity curve *C*-180 eV except for the difference in the peak height. This similarity is well understood from Fig. 11, which shows that the mutual relation among the Bragg conditions 004, 006 and the condition of the 20-rod resonance is similar for *B*-500 eV and *C*-180 eV. In these cases, the  $\bar{4}0$ -rod resonance seems to be not so influential.

The intensity curves in the *B* and *C* azimuths are generally flatter and have less fine structure than those in the *A* azimuth. This is probably because the resonance curves in the *B* and *C* azimuths are more crowded than those in the *A* azimuth.

#### (b) Remarkable enhancement of the peak intensities

In the intensity curves shown in Fig. 3, there are a number of extraordinarily enhanced peaks, such as the 004 peak in the *A* azimuth, the 0,0,10 in *B*-460 eV

and in *C*-300 eV and the 008 peak in *C*-220 eV. These remarkable peaks can be interpreted as follows.

The 004 peak in the *A* azimuth is enhanced by simultaneous participation of the 20- and  $\bar{2}0$ -rod resonances which involve the surface waves 202 and  $\bar{2}02$  belonging to these rods. This effect is especially conspicuous in the energy range from 500 to 340 eV. How-

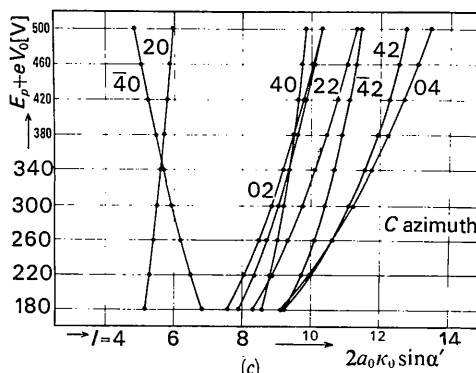
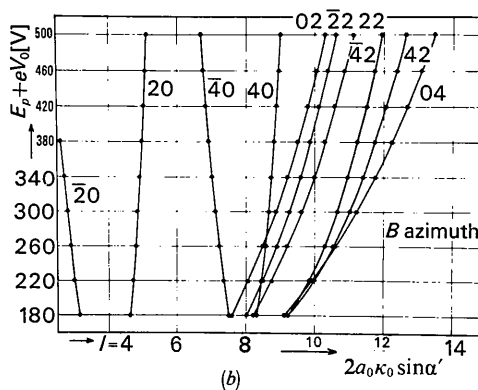
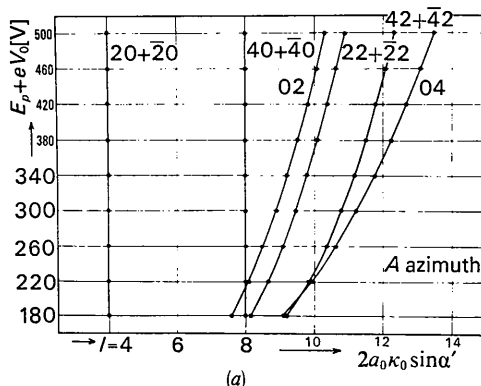


Fig. 11. (a), (b), (c) Calculated resonance curves for *A*, *B* and *C* azimuths. The ordinate is  $E_0 + eV_0$  and the abscissa,  $2a_0\kappa_0 \sin \alpha'$ ,  $\kappa_0$  and  $\alpha'$  are the mean wave number and the glancing angle in the crystal respectively (see the text). Indices '20', for instance, indicate the resonance curve for the 20-rod resonance.



ever, this peak becomes less marked below 340 eV. This seems to suggest that the 202 and  $\bar{2}02$  surface waves are gradually extinguished as the electron energy decreases.

The remarkable intensity of the 0,0,10 peak in *B*-460 eV is apparently due to the coincidence of the Bragg condition 0,0,10 with the 02-rod resonance, as indicated by the 02 resonance curve in Fig. 11(b) (*cf.* Fig. 6 for *B*-500 eV). Similarly, the strong peak 0,0,10 in *C*-300 eV can be ascribed to the coincidence with the 22-rod resonance. The strong peak of 008 in *C*-220 eV is also in coincidence with the 02-rod resonance (*cf.* Fig. 7). The fairly strong intensities of the 008 peak in *C*-180 eV, *A*-220–180 eV and *B*-220–180 eV may also be ascribed to the same situation.

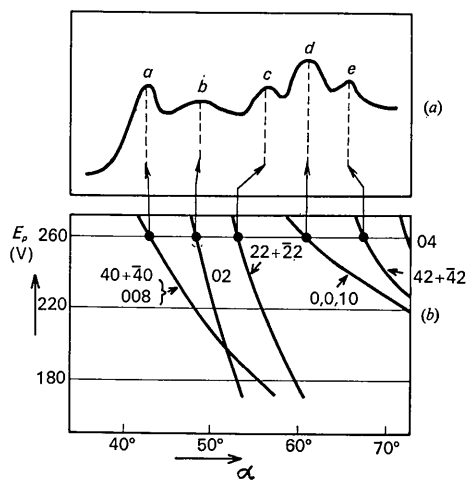


Fig. 12. (a) Fine structure in the intensity curve of *A*-260 eV. (b) A part of Fig. 11(a) converted to a function of  $\alpha$ , assuming the mean inner potential  $V_0 = 14$  V.

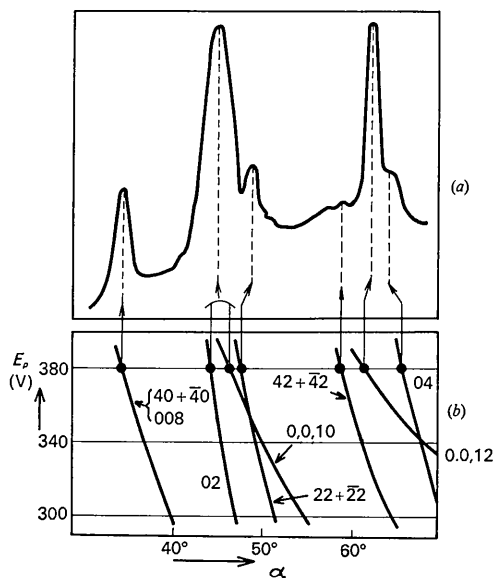


Fig. 13. (a) Part of *A*-380 eV. (b) Part of Fig. 11(a) converted to a function of  $\alpha$ . ( $V_0 = 14$  V).

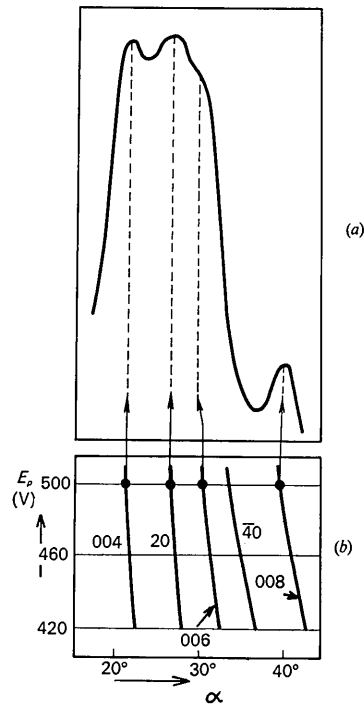


Fig. 14. (a) Part of *B*-500 eV. (b) Part of Fig. 11(b) converted to a function of  $\alpha$ . ( $V_0 = 14$  V).

It is also noted in *B*-220 eV and *C*-220 eV that the 0,0,10 peak is enhanced by the 04-rod resonance.

### (c) Reflexion intensity at the off-resonance condition

Although, as described above, the 004 peak is exceedingly strong in the *A* azimuth, it is not so significant in the *B* azimuth, being comparable with the 006 peak. This abrupt change occurs because the simultaneous condition for the Bragg reflexion 004 and for the 20- and  $\bar{2}0$ -rod resonances is lost in the *B* azimuth.

The 004 peak is depressed still further in the *C* azimuth. On the contrary, the 006 peak which is not so conspicuous in the *A* and *B* azimuths becomes remarkable in the *C* azimuth (*cf.* Fig. 8). This feature can be understood from the behaviour of the 20-rod resonance curve in Fig. 11(c), which runs very close to the vertical line corresponding to the Bragg reflexion 006 over a wide range of electron energy (*cf.* Fig. 8). On the other hand, it is noticeable in the same Figure that there is no resonance curve in the vicinity of the vertical line corresponding to the 004 Bragg condition.

It is the general trend that a Bragg reflexion which is not accompanied by any rod resonance is rather weak. The weak intensities of the 008 peak in *B*-500–300 eV correspond to a similar case.

## 6. Discussion

As known from a number of examples in §5(b)–(c), most of Bragg peaks with appreciable intensities are those which are more or less affected by the existence

of resonance effects. The resonance effect possesses, so to speak, a 'pumping action', by which the waves propagating into the crystal are efficiently converted to outgoing waves. As was calculated for HEED by Kohra, Molière, Nakano & Ariyama (1962), the reflectivity of the specular reflexion enhanced by a resonance effect may nearly attain unity in the non-absorbing case. The pumping action of the resonance effect is very important for the understanding of LEED phenomena in general, since resonance takes place more frequently in LEED than in HEED, mainly because of the small radius of the Ewald sphere in the former case. Consider, for instance, the experimental condition of normal incidence of the electrons at the crystal surface. In this case, the electron scattering in forward directions may efficiently be converted to the backward scattering with scattering angle about  $180^\circ$  through the resonance effect, provided that the effective value of the atomic scattering factor for the  $90^\circ$  scattering is more or less appreciable, even if that for the direct  $180^\circ$  scattering is not so.

In the present paper, it has been shown that some fine structures as well as gross features of the intensity curves can be qualitatively interpreted fairly well in terms of the resonance effect. Naturally, the present

method of analysis is difficult to take over into quantitative interpretation. However, by the present method, it is possible to know which rod resonances have a particular influence on the reflexion intensity in a limited range of electron energy and glancing angle. It is conceived that such information may be used as a guide for theoretical work in order to set up an appropriate approximation in individual cases.

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### Magnetische Struktur des Trirutils $\text{FeTa}_2\text{O}_6$

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By means of neutron diffraction the magnetic structure of  $\text{FeTa}_2\text{O}_6$  has been determined. The observed magnetic reflexions define a unit cell  $2a, b, 2c$ . In order to match the tetragonal symmetry this cell must be enlarged again, which results in the final magnetic cell  $2a, 2b, 2c$  with the magnetic space group  $Ic4_1/a$ . The structure contains two sublattices with the cells  $2a, b, 2c$  and  $a, 2b, 2c$ , the moments of which are perpendicular to each other. The moments lie in the  $a/b$  plane and form an angle of  $\varphi_a = 45^\circ$  with the  $a$  axis. The spin quantum number is found to be  $S = 2.04$ .

#### Einleitung

Von Trirutilen  $\text{AB}_2\text{O}_6$  mit dem magnetischen Kation auf dem A-Platz sind noch keine magnetischen Strukturen bestimmt worden. Bekannt ist aufgrund von Neutronenbeugungsmessungen lediglich, dass die Substanz  $\text{NiTa}_2\text{O}_6$  eine komplizierte magnetische Struktur besitzt, ohne dass die Struktur jedoch bisher gelöst werden konnte (Kunnmann, La Placa, Corliss, Hastings & Banks, 1968). Im folgenden soll über die Bestimmung der magnetischen Struktur des Trirutils  $\text{FeTa}_2\text{O}_6$  aus einem Neutronenbeugungspulverdiagramm berichtet werden. Wohl konnten mit Neutronenbeugung die magnetischen Strukturen von inversen

Trirutilen gefunden werden, nämlich von  $\text{Cr}_2\text{WO}_6$  (Kunnmann *et al.*, 1968; Montmory & Newnham, 1968),  $\text{Cr}_2\text{TeO}_6$  (Kunnmann *et al.*, 1968; Montmory & Newnham, 1968),  $\text{Fe}_2\text{TeO}_6$  (Kunnmann *et al.*, 1968; Montmory, Belakhovsky, Chevalier & Newnham, 1968) und  $\text{V}_2\text{WO}_6$  (Kunnmann *et al.*, 1968). In letzter Zeit ist noch die magnetische Struktur von  $\text{LiFe}_2\text{F}_6$  hinzugekommen (Shachar, Makovsky & Shaked, 1972; Wintenberger, Tressaud & Menil, 1972). In diesen inversen Trirutilen besetzen die magnetischen Kationen den B-Platz, so dass die magnetischen Strukturtypen sich wesentlich von denen der Trirutile unterscheiden müssen. Dagegen sind die bei den Trirutilen zu erwartenden magnetischen Strukturtypen